Math Released Item 2019

Grade 4

Subtraction of Fractions on Number Line Drawing M400439D

Anchor Set A1 – A8

With Annotations

Prompt

Part A

Describe how to show the sum $\frac{3}{8} + \frac{2}{8}$ on the number line shown.



Select from the drop-down menus to correctly complete each sentence.

Divide the segment of the number line between 0 and 1 into	Choose \$	equal parts. Starting at 0,
	3	
	5	
	8	
	10	



Part B

The number line shown can be used to model the expression $\frac{7}{10} - \frac{3}{10}$.



- To model the expression, how many parts should the segment of the number line between 0 and 1 be divided into? Explain your answer.
- Describe each of the remaining steps needed to model the expression.
- · What is the value of the expression?

Enter your answers, your explanation, and your description in the space provided. You may use the drawing box to add a drawing to help explain your answer.



Drawing Box



M04_M400439 Rubric- Part A (Machine Scored)				
Score	Description			
	This part of the item is machine scored.			
	• Reasoning component = 1 point:			
1	$_{\odot}$ Divide the segment of the number line between 0 and 1 into			
	$\underline{8}$ equal parts. Starting at 0, shade the first $\underline{3}$ parts. Then,			
	shade the part 2 parts to show the sum of $\frac{3}{2} + \frac{2}{2}$			
	shade the flext $\underline{2}$ parts to show the sum of $\underline{-}$ + $\underline{-}$ 8 8			
0	Student response is incorrect or irrelevant.			
M04 M400439 Rubric- Part B				
Score	 Description			
	Student response includes each of the following 3 elements.			
	- Beaconing component - 1 point:			
	• Reasoning component = 1 point.			
	 Valid explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts 			
	between o and i needs to be divided into io equal parts			
	• Reasoning component = 1 point:			
	\circ Valid description of each of the remaining steps needed to			
	model the expression			
	 Computation component = 1 point: 			
3	\circ Correct value of the expression, $\frac{4}{10}$ or equivalent			
	Student Sample Response:			
	The compart of the number line between 0 and 1 should be			
	divided into 10 equal parts because the denominators in the			
	expression are 10.			
	Starting at zero, shade the first 7 parts. Then, erase 3 of those			
	4 · · · · · · · · · · · · · · · · · · ·			
	$\frac{1}{10}$ is the value of the expression.			
	Or other valid response			
2	Student response includes 2 of the 3 elements.			
1	Student response includes 1 of the 3 elements.			
0	The response is incorrect or irrelevant.			





Anchor Paper 1 Score Point 3

This response receives full credit. It includes each of the three required elements.

 A valid explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is provided (There should be 10 line segments between the 0 and the 1 because the denominator is 10 and the denominator shows how many equal parts there are in 1 whole).

Note: Students are not required to use the term "equal" in their explanations for this element. The prompt includes the term "divide", which clearly establishes the expectation of equal parts. However, they are expected to tie the need for 10 segments to the denominator.

- A valid description of each of the remaining steps needed to model the expression is provided (you shade 7 parts out of the 10 parts. Next, you shade 3 parts out of the 7 parts . . . Lastly, you count the lines that you haven't shaded). In addition, the student has provided a drawing that shows the shading of 7 parts, the second overlay shading of 3 out of the 7 parts (which look like back slashes) and, finally, the counting of the parts without the second layer of shading (4, 3, 2, 1). The written description or the drawing alone satisfies this element.
- The correct value of the expression is provided $\left(\frac{4}{10}\right)$.





Anchor Paper 2 Score Point 3

This response receives full credit. It includes each of the three required elements.

• A valid explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is provided (10 parts because the denominator is 10).

Note: Students are not required to use the term "equal" in their explanations for this element. The prompt includes the term "divide", which clearly establishes the expectation of equal parts. However, they are expected to tie the need for 10 segments to the denominator.

• A valid description of each of the remaining steps needed to model the expression is provided (plot the seventh parts. Then, go back three of them. Whatever you land on is your answer). In addition to this explanation, the student provides a number line in the drawing box that clearly shows a number line divided into 10 parts. $\frac{7}{10}$ is marked with a large dot, and the three jumps back from that point land on $\frac{4}{10}$, which is circled. The written description or the drawing alone satisfies this element.

• The correct value of the expression is provided $\left(\frac{4}{10}\right)$.





Anchor Paper 3 Score Point 2

This response receives partial credit. It includes two of the three required elements.

- A valid explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is provided (You would have to devide the number line into 10 parts becauses the fractions are tenths). While the student does not use the term "denominator", the use of the mathematically specific term "tenths" clearly ties the number of parts to the denominator.
- A valid description of each of the remaining steps needed to model the expression is provided (Then you would have to shade 7 of the parts starting at 0. Last you would have to cross out 3 parts wich leaves you with 4 shaded parts). On the number line in the drawing box, the student crosses out $\frac{3}{10}$ starting at 0 rather than $\frac{7}{10}$; however, this strategy is valid since the parts not crossed out can be counted to find the solution.

The value of the expression is incorrect. While the student references 4 parts (wich leaves you with 4 shaded parts), the correct fraction with a numerator and denominator is required in order to receive credit for this element.

Anchor Paper 4 Score Point 2

This response receives partial credit. It includes two of the three required elements.

- A valid description of each of the remaining steps needed to model the expression is provided (shade in $\frac{7}{10}$ of the number line then erase $\frac{3}{10}$ of $\frac{7}{10}$ then we find the diffrence). In addition to this explanation, the student provides a number line in the drawing box that shows a valid strategy of marking $\frac{7}{10}$ and moving back $\frac{3}{10}$ to land on $\frac{4}{10}$.
- The correct value of the expression is provided $\left(\frac{4}{10}\right)$.

The explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is not tied to the denominator so is not sufficient to receive credit (it should be divided in 10 equal parts). Students must tie the reason for the number of parts to the denominator of the fractions.

Anchor Paper 5 Score Point 1

This response receives partial credit. It includes one of the three required elements.

• A valid explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is provided (you would make the number line between 0 and 1 divided into 10 because 10 is your denomonaters).

The description of each of the remaining steps needed to model the expression is incorrect (then you would add 7 and 3 and get 10). This description does not use the number line, and it incorrectly describes addition rather than subtraction.

The value of the expression is incorrect $\left(\frac{10}{10}\right)$.

Anchor Paper 6 Score Point 1

This response receives partial credit. It includes one of the three required elements.

• A valid description of each of the remaining steps needed to model the expression is provided (you shade in seven parts then you erase three parts).

The explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is not tied to the denominator so is not sufficient to receive credit (you break it up into 10 equal pecies).

The correct value of the expression is not provided.

Anchor Paper 7 Score Point 0

This response receives no credit. It includes none of the three required elements.

The explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is not tied to the denominator, therefore it is not sufficient to receive credit (The number line should be divided into 10).

No description of each of the remaining steps needed to model the expression is provided.

The correct value of the expression is not provided.

Anchor Paper 8 Score Point 0

This response receives no credit. It includes none of the three required elements.

No explanation why the segment of the number line between 0 and 1 needs to be divided into 10 equal parts is provided.

No description of each of the remaining steps needed to model the expression is provided.

The value of the expression is incorrect (4). While the student provides the number 4, which is the correct numerator, the denominator is not included in the solution to the expression. The difference must include both the numerator and denominator in order to receive credit for this element.

Practice Set P1 - P5

No Annotations Included

Practice Set

Paper	Score
P1	2
P2	1
Р3	2
P4	3
P5	2